

# Developments in Atmospheric Science 22

R. BURMAN AND L.O. POCHOP

## Evaporation, Evapotranspiration and Climatic Data



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# EVAPORATION, EVAPOTRANSPIRATION AND CLIMATIC DATA

R. BURMAN  
L.O. POCHOP

*University of Wyoming  
Department of Civil and Architectural Engineering  
College of Engineering  
P.O. Box 3295  
Laramie, Wyoming 82071-3295  
U.S.A.*

301/5706 INSTITUT  
FÜR METEOROLOGIE U. KLIMATOLOGIE  
UNIVERSITÄT HANNOVER  
HERRENHÄUSER STR. 2 - 30419 HANNOVER



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